

# DARK MATTER PARTICLE PHYSICS

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# Plan of the lectures

- Dark Matter (DM) candidates
  - Baryonic & non-baryonic
- DM relic density
  - Brief derivation
  - Hot and cold relics
- DM and New Physics
  - Supersymmetric Models (briefly)
  - Neutralino DM
- Direct neutralino DM detection
  - Main formulae
  - Results
- Indirect neutralino DM detection
  - Propagation of charged particles
  - Gamma-ray
  - Results

# Matter & Energy in the Universe

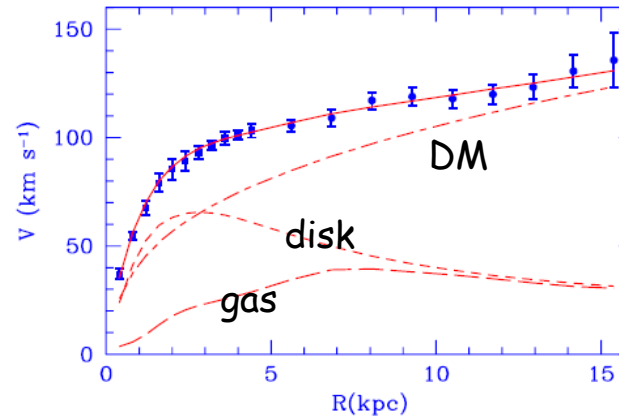
(See Lectures by Goobar and Djorgovski)

Galactic: rotation curves

$$\Omega_{\text{lum}} \sim 0.01 \quad (\text{stars\&gas})$$

$$\Omega_{\text{halo}} \sim 0.1 \quad (\text{DM})$$

M33 RC (Corbelli & Salucci) 1999



Extragalactic:

$$\Omega_m \sim 0.2-0.3$$

Clusters of galaxies

galaxy motions (optical)

temperature of hot cluster gas (X-ray)

gravitational lenses to bkgd objects

Lyman- $\alpha$  (absorption features in QSO)

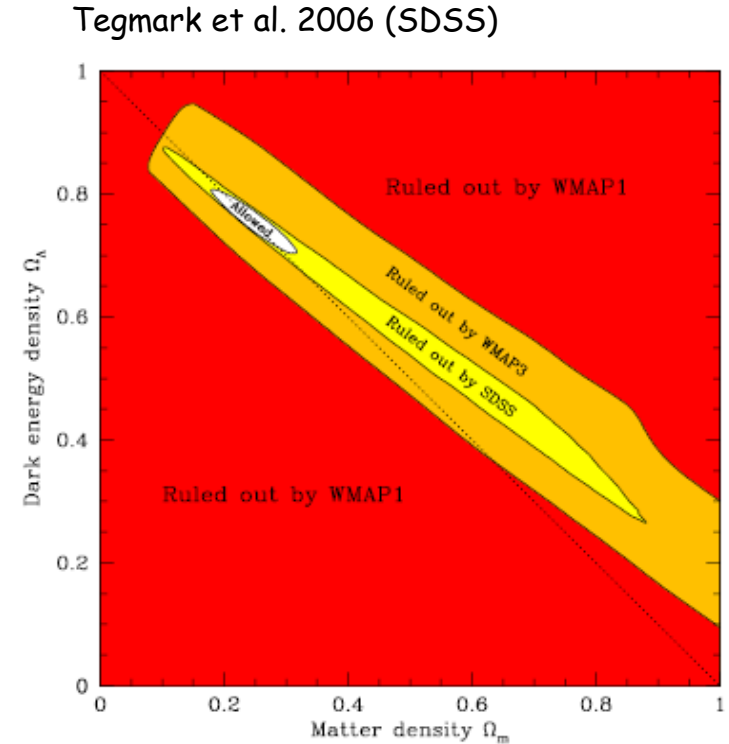
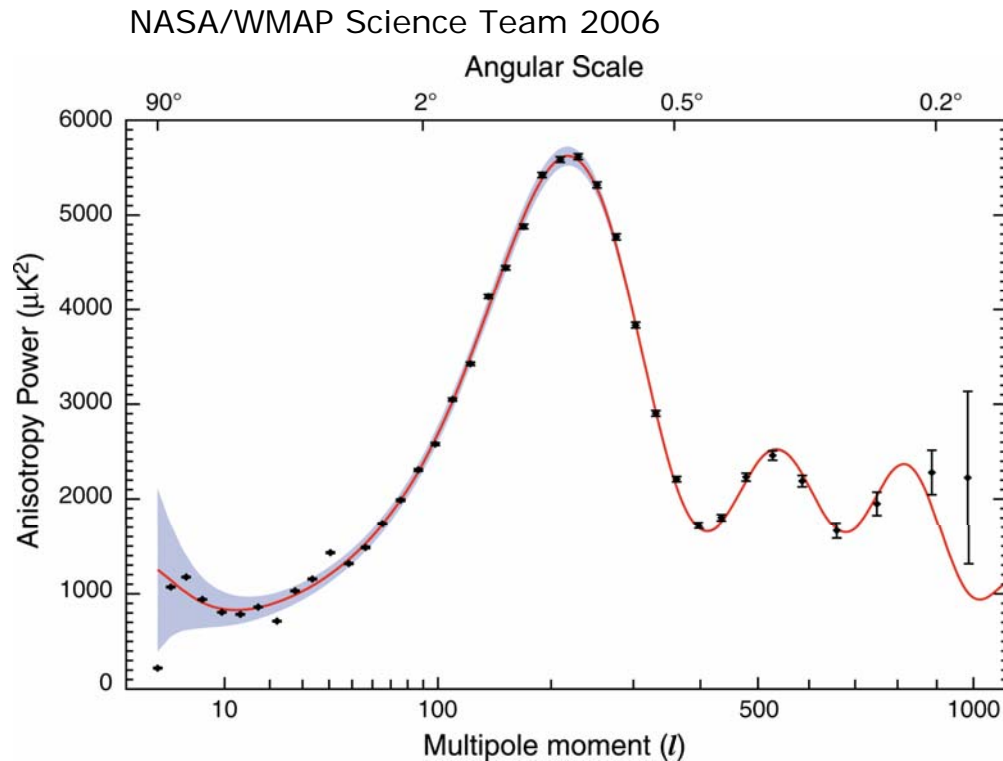
# Cosmological scales: CMBR, SNIa, LSS

$$\Omega_m h^2 = 0.127^{+0.007}_{-0.013}$$

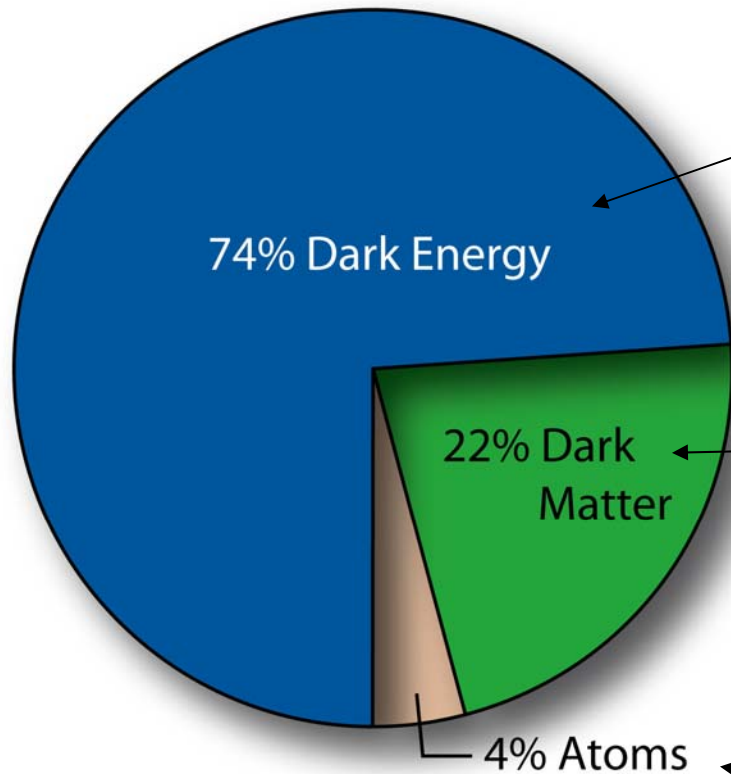
$$\Omega_b h^2 = 0.0223^{+0.0007}_{-0.0009} \text{ (WMAP)}$$

$$\Omega_{\text{tot}} = 1.003 \pm 0.010 \text{ (WMAP\&SDSS)}$$

$$\Omega_m \sim 0.24 \quad \Omega_\Lambda \sim 0.76 \text{ (WMAP\&SDSS)}$$



# Universe Pie



A MISTERY!  
See Lectures by Doran...☺

MOSTLY A MISTERY!  
Stay with us!  
We're going to share  
Hopes ☺ and dark thoughts ☹

Standard Model of Particle Physics  
MOSTLY UNDERSTOOD...

# Candidates to Dark Matter

- **Non-"luminous" baryons**

Jupiters, white dwarfs, remnants of massive stars:

MACHOs (gravitational lensing)

primordial black holes (evaporation products)

diffused (intragalactic or intracluster) hydrogen (abs. lines)

- **Non-baryonic DM**

Massive neutrino

Axion

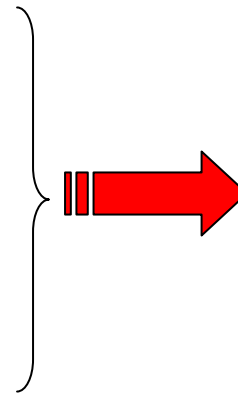
**Neutralino**

Kaluza Klein particle

Gravitino, axino, sneutrino, ....

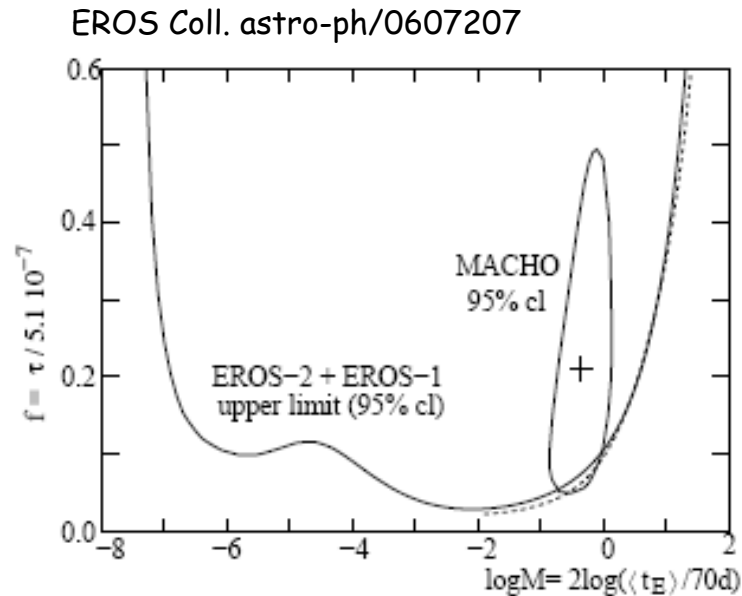
Q-balls, little Higgs, .....

Ultra heavy ????



**new particles,  
New Physics!!**

# Baryonic DM: limits



Baryonic dark matter  
must be compatible with BBN  
predictions  $0.017 \leq \Omega_b h^2 \leq 0.024$

Neutral hydrogen clouds seen  
in Lyman- $\alpha$  forests

Density comparable to the one  
required by BBN

Fraction of dark massive halo objects  
(machos) is small ( $< 10\%$ ).  
MACHO Coll. results different  
Self lensing?

# Non-baryonic DM

- Relics from early universe
- STABLE on cosmological scales
- Particles in thermal equilibrium with the primordial plasma (thermal relics)
  - HOT DM: relativistic when decoupling
  - COLD DM: non-relativistic when decoupling
- WIMP: Weakly Interacting Massive Particles
- Have right relic density

# Relic Density

## Equilibrium Thermodynamics

A weakly interacting particle gas in thermodynamical equilibrium:

number density:  $n = \frac{g}{(2\pi)^3} \int f(\vec{p}) d^3 p$

energy density:  $\rho = \frac{g}{(2\pi)^3} \int f(\vec{p}) E(\vec{p}) d^3 p$

$g$  internal degrees of freedom

$f(p)$  phase space distribution func.  $f(\vec{p}) = \frac{1}{e^{(E-\mu)/T} \pm 1}$

$\pm$  Fermi-Dirac/Bose-Einstein,  $\mu$  chemical potential (assumed to be zero)

Rel. limit ( $T \gg m$ ):  $n \propto T^3, \rho \propto T^4$

Non-rel. Limit ( $T \ll m$ ):  $n \propto T^{3/2} \exp(-m/T)$

# Decoupling from the primordial plasma

Consider a stable particle  $\chi$

In case of no plasma- $\chi$  interaction, the number of  $\chi$  particles for comoving volume  $Y_\chi \equiv n_\chi / s$  is constant. \*

**Annihilation processes** may let  $Y_\chi$  change:  $\chi\bar{\chi} \rightarrow X\bar{X}$

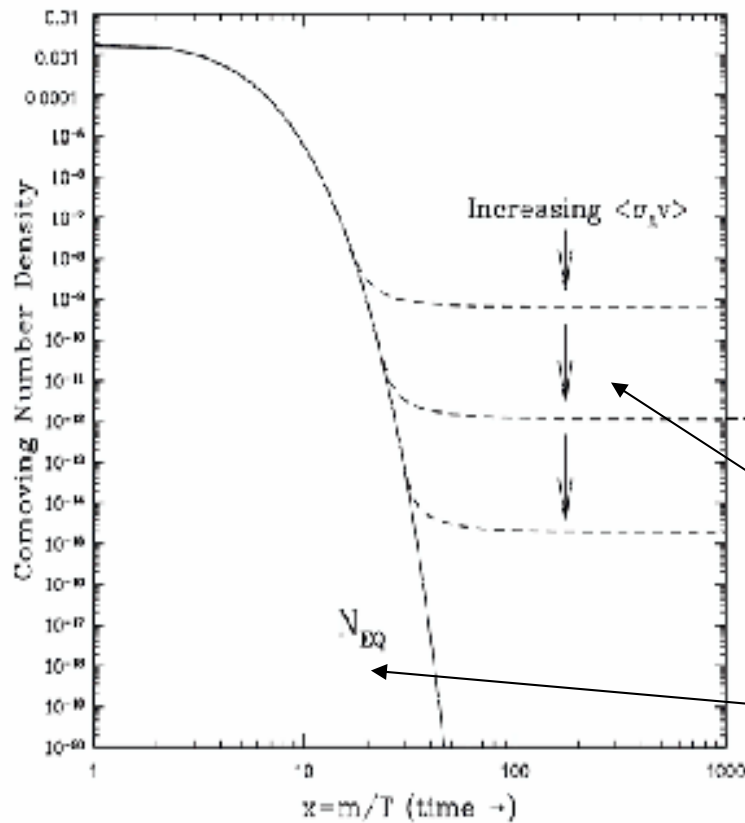
They let the species  $\chi$  in thermic equilibrium until  $\Gamma/H > 1$  ( $\Gamma$  is the collision term,  $H$  the Hubble parameter)

When  $\Gamma/H \ll 1$  expansion dominates and the annihilation freezes, at the **freeze-out** temperature  $T_f$

\*Entropy per comoving volume:  $S = (p + \rho)R^3/T$

Entropy density:  $s \equiv S/R^3$  (In thermodynamic equilibrium  $S$  is constant)

Decoupling from the plasma takes place when  $T$  is sufficiently low, namely when expansion ( $H$ ) dominates over collisions ( $\Gamma$ ).



$$\Gamma_{\text{ann}} = n_{\chi} \langle \sigma_{\text{ann}} v \rangle$$

$$n_{\text{EQ}} \propto T^3 \text{ relativistic}$$

$$n_{\text{EQ}} \propto (mT)^{3/2} \exp(-m/T) \text{ non-relativistic}$$

*Departure from equilibrium*

*Equilibrium*

# Boltzmann Equation

$$\frac{dn}{dt} + 3Hn = \frac{g}{(2\pi)^3} \int C(f) \frac{d\vec{p}}{E}$$

$C(f)$  collision term  $\rightarrow$  annihilation:  $\Gamma_{ann} = n_\chi \langle \sigma_{ann} v \rangle$

$$\frac{dn_\chi}{dt} + 3Hn_\chi = - \langle \sigma_{ann} v \rangle_{TOT} [n_\chi^2 - (n_\chi^{EQ})^2]$$

Dilution effect  
due to expansion

Destruction rate

Inverse creation  
Processes at equil.

$$\frac{x}{Y_{EQ}} \frac{dY}{dx} = - \frac{\Gamma_{ann}}{H} \left[ \left( \frac{Y}{Y_{EQ}} \right)^2 - 1 \right]$$

$$x = m/T$$

$\Gamma_{ann}/H \ll 1$  **freeze-out** of the species at  $T_f$

$T \ll m$  creation processes are Boltzmann suppressed

$\Gamma_{ann}$  decreases with  $T$  up to when annihilations become ineffective

# HOT and COLD relics

HOT relic particles:  $x_f \equiv m/T_f \ll 3$  (high T, low m)

Decoupling arrives when particles are still relativistic  $Y=n/s \sim T^3 R^3 \sim \text{const}$   
Details of freezing are not much relevant

$$Y(x \rightarrow \infty) \equiv Y_{EQ}(x_f) = 0.278 \frac{g_{eff}}{g_{*s}(x_f)}$$

$$\rho_{\chi 0} \equiv s_0 Y_{\infty} m = 2.97 \cdot 10^3 Y_{\infty} (m/eV) \quad \text{eV/cm}^3$$

$$\Omega_{\chi} h^2 = 7.83 \cdot 10^{-2} \frac{g_{eff}}{g_{*s}(x_f)} \frac{m}{\text{eV}}$$

For light neutrinos:  
 $g_{*s}=10.75, g_{eff}=2 \cdot 3/4 \rightarrow$

$$\Omega_{\nu} h^2 = \frac{\sum m_{\nu}}{93.1 \text{ eV}}$$

**Neutrino  
relic density**

# Neutrino DM

Several evidences for neutrinos to be **massive** come from different neutrino oscillation experiments (depending only on mass differences)

- **atmospheric** neutrinos (Kamiokande, SK, Macro, ...)  
 $|\Delta m_{\text{ATM}}|^2 \sim 2.5 \cdot 10^{-3} \text{ eV}^2$
- **solar** neutrinos (SNO, SK, Kamiokande, Gallex, GNO, ...)  
 $|\Delta m_{\text{SUN}}|^2 \sim 8 \cdot 10^{-5} \text{ eV}^2$
- **Reactor** (Chooz) and **accelerator** (K2K, Minos) experiments:  
 $|\Delta m|^2 \sim |\Delta m_{\text{ATM}}|^2$

Upper limits on neutrino masses come from  $\beta$  decay expts. indicate eV scale masses

Light neutrinos



**HOT DARK MATTER**

# Cosmological neutrinos

Neutrino DM - depending on the mass - washes out the power spectrum of primordial density perturbations, and suppresses the formation of the observed structures at 1-10 Mpc scales.

Limits to  $\Sigma m_\nu$  from CMBR experimets (WMAP), Large Scale Structures (SDSS, 2dFGRS), Lyman  $\alpha$  forests.

Data Set	$\Sigma m_\nu$ (95% limit for $N_\nu = 3.02$ )	$N_\nu$
WMAP	2.0 eV(95% CL)	
WMAP + SDSS	0.91 eV(95% CL)	$5.92^{+0.25}_{-3.45}$
WMAP + 2dFGRS	0.87 eV(95% CL)	$2.68^{+0.26}_{-1.67}$
CMB + LSS +SN	0.68 eV(95% CL)	$3.29^{+0.45}_{-2.18}$

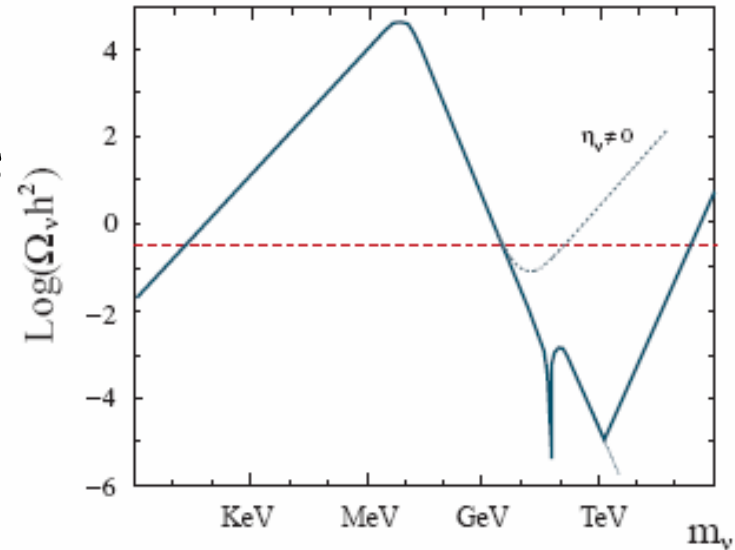
(Spergel et al. astro-ph/0603449)

CMB+Lyman  $\alpha$ :

$$\underline{\underline{\Sigma m_\nu < 0.30 eV}}$$

(Goobar et al. 2006)

Neutrino relic density  
 Cosmological limits on neutrino mass  
 Overdensity for a wide range of mass



$$\text{From WMAP } \Omega_{\nu} h^2 = \frac{\sum m_{\nu}}{93.1 \text{ eV}} \leq 0.0073$$

Only a very small fraction of  $\Omega$  can be ascribed to massive neutrinos

**WE NEED COLD DARK MATTER (CDM)**

*The Universe is most probably a mixture of  
several kinds of dark components*

**COLD** relic particles:  $x_f \equiv m/T_f \gg 3$  (low  $T$ , high  $m$ )

Decoupling arrives when massive particles are no more relativistic.

Details of freezing and annihilation are important.

$$\frac{dY}{Y^2} \cong -0.264 \frac{g_{*s}}{g_*^{1/2}} m_{Pl} \frac{m}{x^2} \langle \sigma v \rangle dx$$

Integrating from  $T_f$  to  $T=0$ :  $\Omega_\chi h^2 \cong 3.3 \cdot 10^{-38} \frac{g_*(x_f)^{1/2}}{g_{*s}(x_f)} \frac{cm^2}{\langle \sigma v \rangle_{int}}$

$x_f \approx 20, g_*(x_f) \approx g_{*s}(x_f) \approx 60$ :  $\Omega_\chi h^2 \approx \frac{4.3 \cdot 10^{-39} cm^2}{\langle \sigma v \rangle_{int}}$

$\langle \sigma_{ann} v \rangle = \sigma_0 (T/m)^n = \sigma_0 x^{-n}$   
 (s wave  $n=0$  p wave  $n=1$ )

**Particle Physics  
 ...New Physics...!**

**EW size!!**

# Supersymmetry & Dark Matter

(See Lectures by A. Masiero)

Fermions  $\Leftrightarrow$  Bosons

R=1

R= -1

Leptons & Quarks

*Sleptons, Squarks*

Gauge Fields

*Gauginos*

Higgs Fields

*Higgsinos*

R-parity conservation:

The Lightest Supersymmetric Particle (LSP) is stable on cosmological scales and can be the Dark Matter!

# Neutralino as the CDM candidate

$$\chi = a_1 \tilde{B}_0 + a_2 \tilde{W}_0^3 + a_3 \tilde{H}_0^1 + a_4 \tilde{H}_0^2$$

- **Stable** (if R-parity is conserved)
- **Mass:**  $m_\chi \sim 10\text{-}1000 \text{ GeV}$
- Non-relativistic at decoupling  $\Rightarrow$  **CDM**
- **Neutral & colourless**
- **Weakly interacting (WIMP)**
- Good relic density  $\Omega_\chi h^2$

# Which Supersymmetric Model?

(See Lectures by A. Masiero)

- Theoretical and experimental constraints are **too faint** to outline a model
- Minimal Supersymmetric extension of the Standard Model (**MSSM**) depends on the **SYMMETRY BREAKING** mechanism:
  - Gravity mediated → **neutralino** DM
  - Gauge mediated → gravitino DM
  - Anomaly mediated → neutralino, stau sneutrino
- The nature and phenomenology of LSP depends on susy breaking and regions of the susy parameter space

# Gravity mediated SUSY schemes

## Supergravity inspired models (SUGRA)

- Unification conditions occur at the GUT scale ( $M_{GUT} \sim 10^{16}$  GeV)

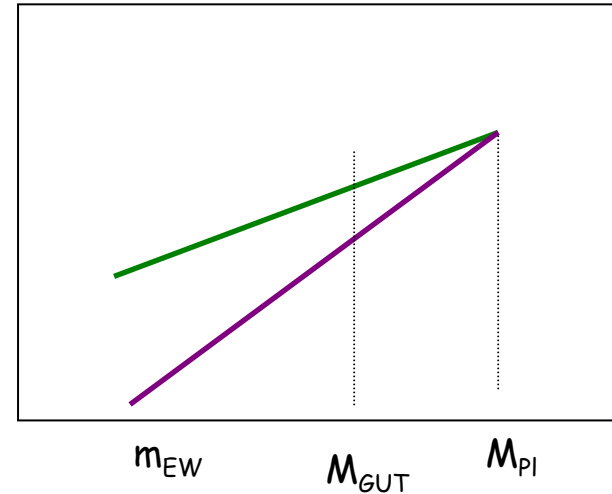
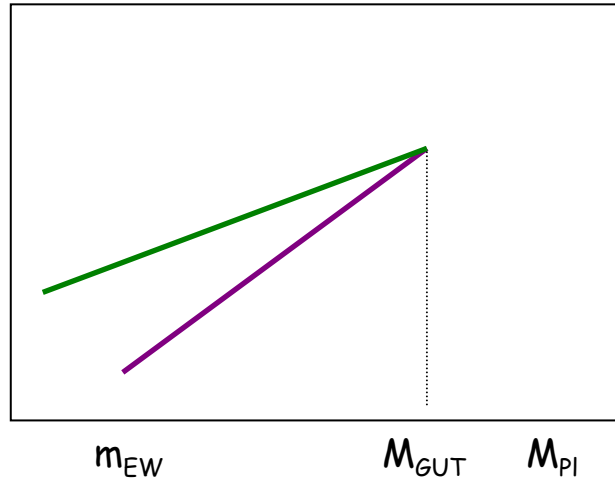
$$M_i(M_{GUT}) = m_{1/2} \quad (\text{gaugino masses})$$

$$m_i(M_{GUT}) = m_0 \quad (\text{scalar masses})$$

$$A^{u(d,l)}(M_{GUT}) = A_0 m_0 \quad (\text{trilinear terms})$$

- Free parameters of the model:  $m_{1/2}, m_0, A_0, \text{sign}(\mu), \tan \beta$
- RGE evolution down to EW scale & radiative EW symmetry breaking

SUGRA is severely constrained by unification assumptions at  $M_{GUT}$ .

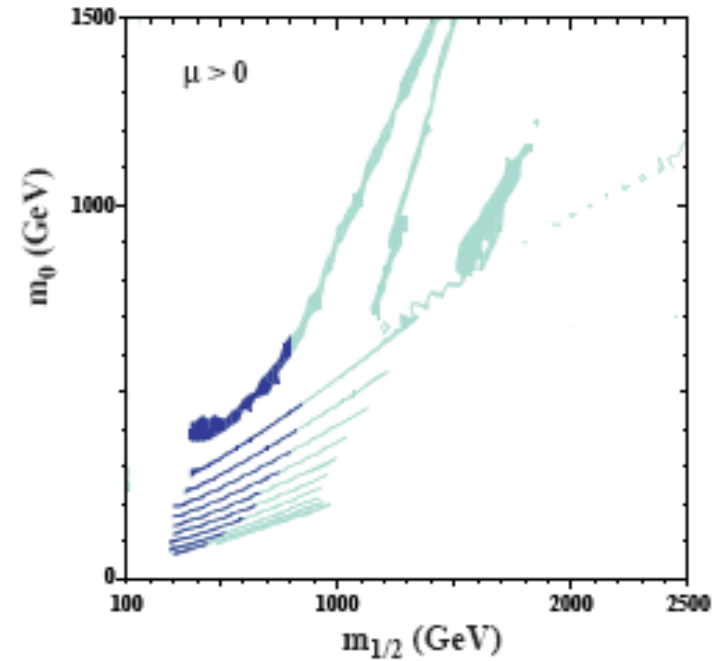
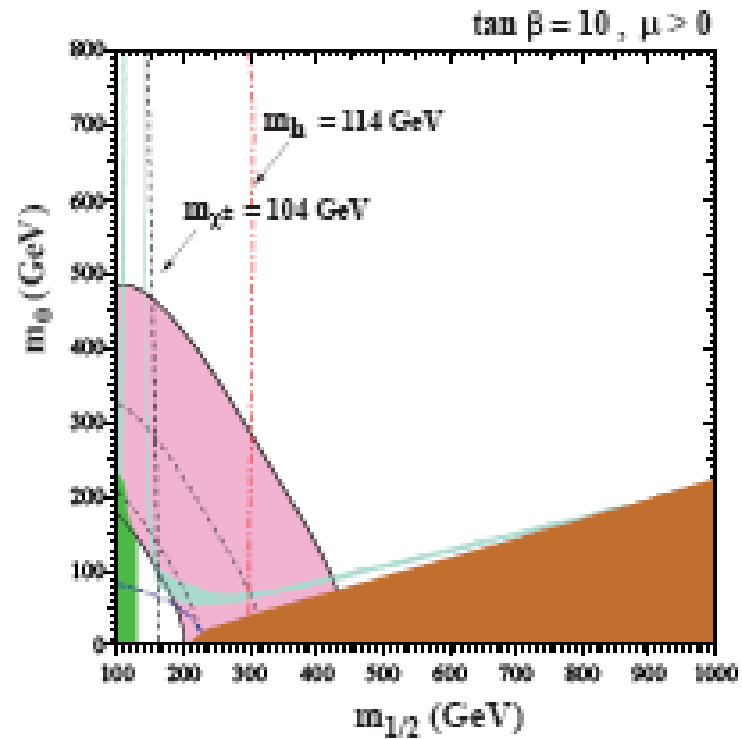


But:

- universality might occur at higher scales ( $M_{plank}$ ) leading to deviations from universality at  $M_{GUT}$
- the starting point for RGE could begin at a lower scale, between  $M_{GUT}$  and  $M_{EW}$

→ non-universal SUGRA

# SUGRA models



Different  $\tan \beta$ : 5, 10, ..., 55

Light blue regions: allowed region

CMSSM Olive astro-ph/0503065

# Effective MSSM scheme (effMSSM)

Model (parameters) defined at the EW scale

## Independent parameters:

- $M_1$  U(1) gaugino soft breaking term
- $M_2$  SU(2) gaugino soft breaking term
- $\mu$  Higgs mixing mass parameter
- $\tan \beta$  ratio of two Higgs v.e.v.'s
- $m_A$  mass of CP odd neutral Higgs boson
- $m_q$  soft mass common to all squarks
- $m_l$  soft mass common to all sleptons
- $A$  trilinear parameter ( $A_b = A_t \equiv Am_q$ ;  $A_\tau \equiv Am_l$ )
  - $R \equiv M_1/M_2$  (=0.5 in GUT)

# Experimental constraints

- EXPERIMENTAL BOUNDS:

- Accelerator (LEP & Tevatron) data on Higgs and supersymmetric particle (negative) searches

- $b \rightarrow s\gamma$

- $B_s \rightarrow \mu^+ \mu^-$  ( $\text{BR}(B_s \rightarrow \mu^+ \mu^-) \leq 9.5 \times 10^{-7}$ )

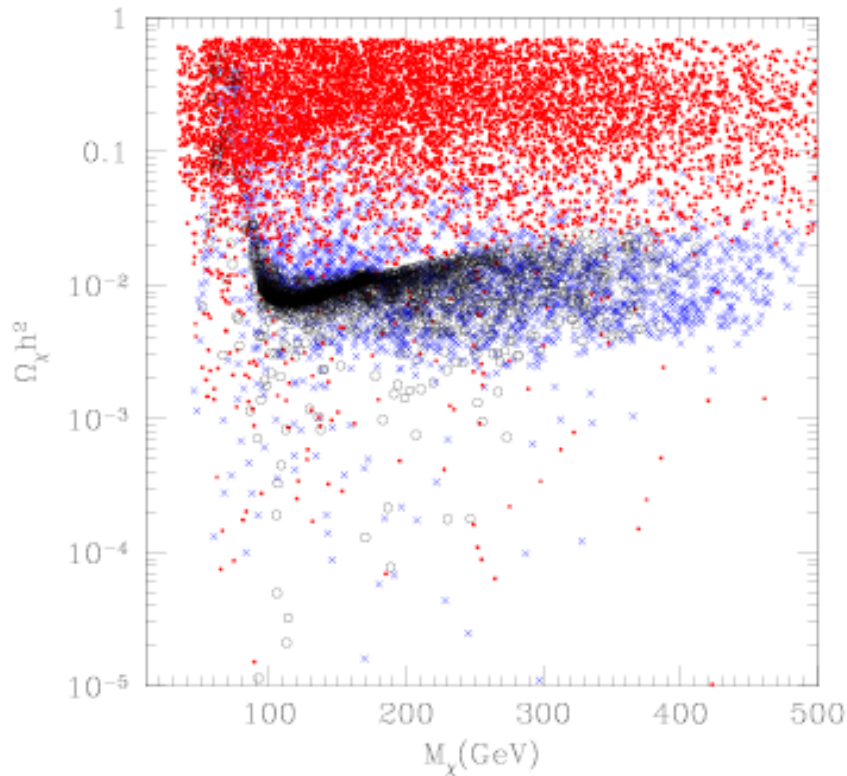
- $a_m \equiv (g_m - 2)/2$  ( $-142 \leq \Delta a_m \cdot 10^{11} \leq 474$ )

- Requirements that neutralino is the LSP

- No a priori on the relic density  $\Omega_\chi h^2$

*Subdominant neutralinos, if detectable, could be very interesting for particle physics (new physics) and cosmology (mixture of candidates)*

# Neutralino relic abundance



*effMSSM* Bottino et al. 2001

The Neutralino can be THE DM candidate ( $\Omega_\chi h^2 \sim 0.1$ ), able to explain the whole non-baryonic DM or a subdominant relic Particle

Red: gaugino

Blue: mixed

Black: higgsino

Upper bound on  $\Omega_\chi h^2 \Rightarrow$  lower bound on  $m_\chi$

Full scanning of **effMSSM**

A. Bottino, F. Donato, N. Fornengo, S. Scopel (2009)

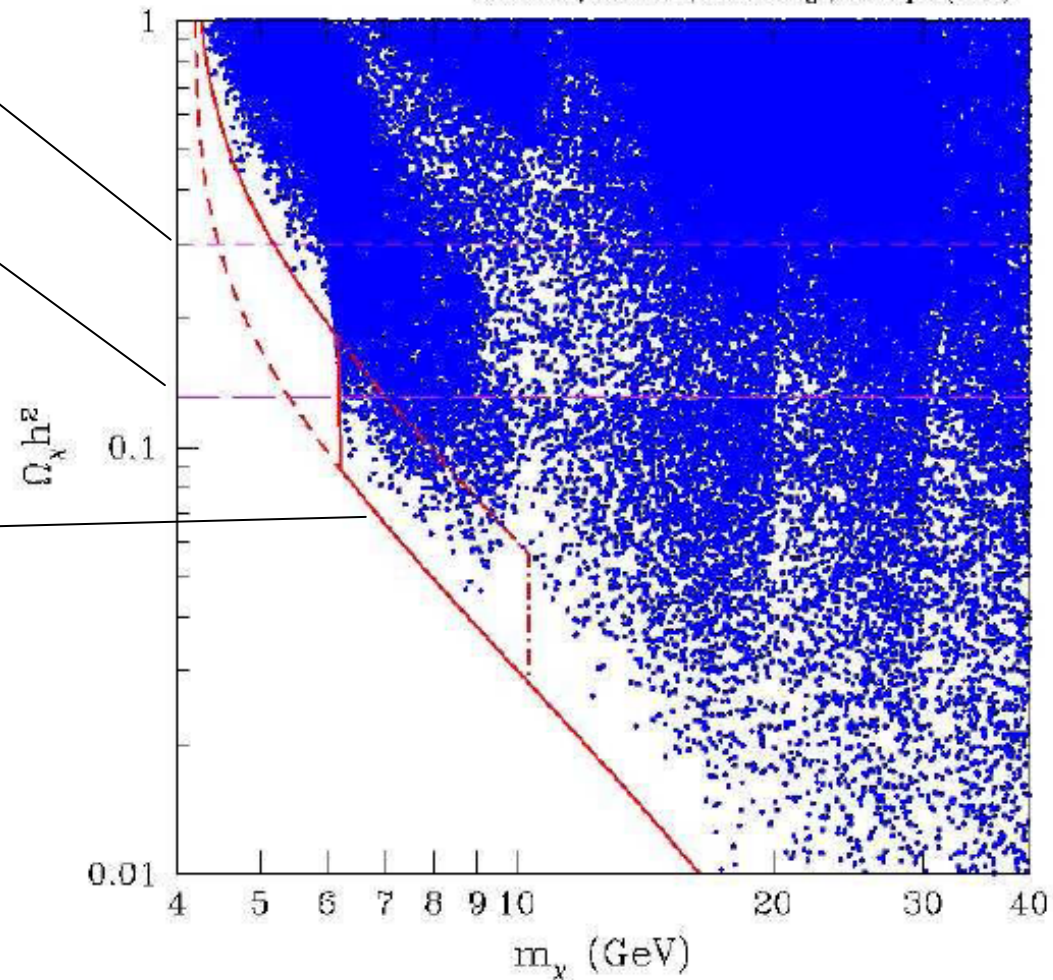
$$\Omega_{\text{CDM}} h^2 = 0.3$$

$$\Omega_{\text{CDM}} h^2 = 0.131 \Rightarrow m_\chi \geq 6.2 \text{ GeV}$$

$$(\Omega_\chi h^2)_{\text{min,Higgs}}^\infty$$

$$((2m_\chi)^2 - m_A^2)^2 / m_\chi^2 \sqrt{1 - (m_b/m_\chi)^2}$$

$$T_{\text{QCD}} = 300 \text{ MeV}$$



# Full scanning of *effMSSM* & $m_A > 300$ GeV

$$\Omega_{\text{CDM}} h^2 = 0.3$$

$$\Omega_{\text{CDM}} h^2 = 0.131 \Rightarrow m_\chi \geq 22 \text{ GeV}$$

$$(\Omega_\chi h^2)_{\text{min, sfermion}}^\infty$$

$$m_{\text{stau}} / m_\chi^2 \sqrt{1 - (m_\tau / m_\chi)^2}$$

$$T_{\text{QCD}} = 300 \text{ MeV}$$

